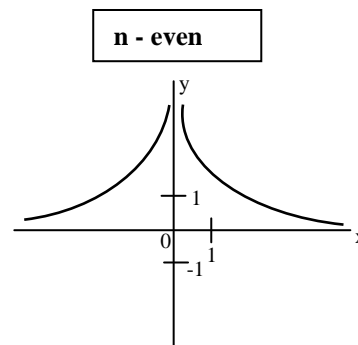
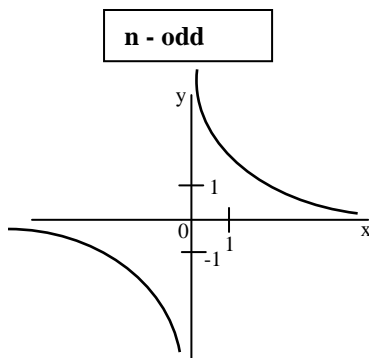


Worksheet 9 – POWER FUNCTION WITH NEGATIVE NATURAL EXPONENT $y = x^{-n}; n \in \mathbb{N}$



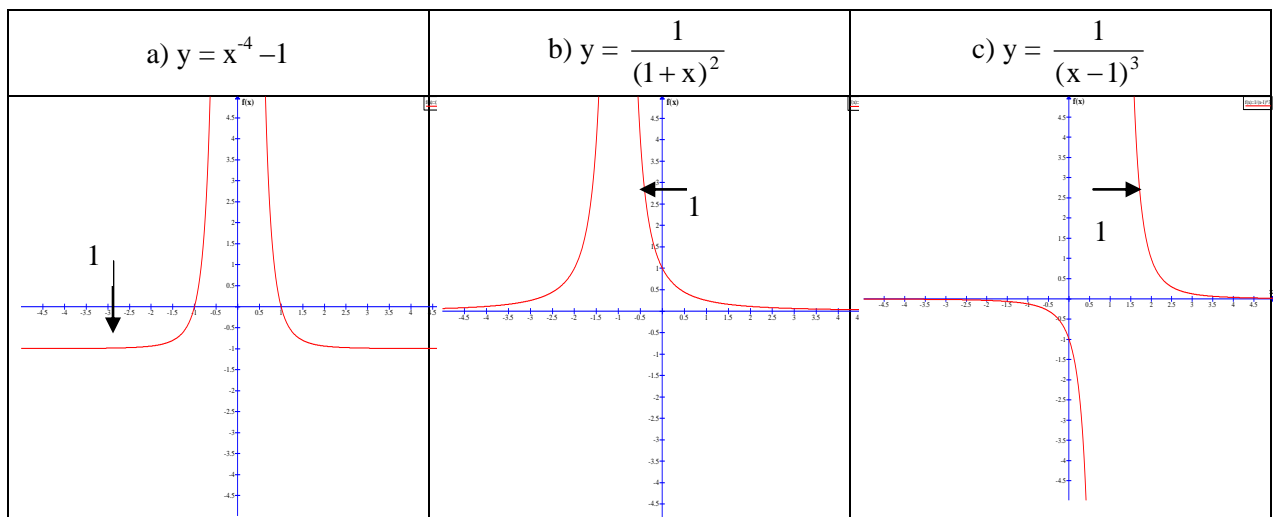
Domain = $\mathbb{R} - \{0\}$

- Range = $\mathbb{R} - \{0\}$
- Decreasing on the intervals $(-\infty, 0), (0, \infty)$
- Not bounded above neither below
- Odd

- Range = \mathbb{R}^+
- Decreasing on the interval $(0, \infty)$
- Increasing on the interval $(-\infty, 0)$
- Not bounded above,
- Bounded below
- Even

No maximum, no minimum

Examples: Draw graphs of functions a) $y = x^{-4} - 1$, b) $y = \frac{1}{(1+x)^2}$, c) $y = \frac{1}{(x-1)^3}$



Exercise: Draw graphs of these functions and write properties:

a) $y = -\frac{1}{x}$, b) $y = -\frac{1}{x} - 1$, c) $y = -\frac{1}{x+2}$, d) $y = -\frac{1}{x+2} - 1$, e) $y = \frac{1}{2x}$, f) $y = \frac{1}{2x} + 2$, g) $y = \frac{1}{2x-1}$, h) $y = \frac{1}{2x+1} + 2$