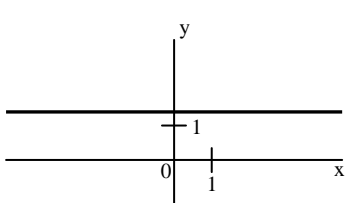
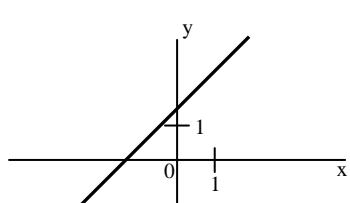
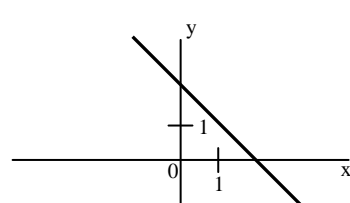


## Math Worksheet 4 – LINEAR FUNCTION

**Basic formula:**  $y = ax + b$

$$a = \text{gradient, } a = \frac{y_2 - y_1}{x_2 - x_1}$$

$b$ - interception with  $y$ -axis

<b>a = 0</b>	<b>a &gt; 0</b>	<b>a &lt; 0</b>
		
<ul style="list-style-type: none"> <li>- Domain = R</li> <li>- Range = {b}</li> <li>- It's one to many,</li> <li>- It's not one to one and therefore it's not increasing neither decreasing</li> <li>- Bounded</li> <li>- In each point <math>x \in R</math> there is maximum and minimum</li> </ul>	<ul style="list-style-type: none"> <li>- Domain = R</li> <li>- Range = R</li> <li>- It's one to one</li> <li>- It's increasing</li> <li>- Not bounded above, neither bounded below</li> <li>- It has no maximum neither minimum</li> </ul>	<ul style="list-style-type: none"> <li>- Domain = R</li> <li>- Range = R</li> <li>- It's one to one</li> <li>- It's decreasing</li> <li>- Not bounded above, neither bounded below</li> <li>- It has no maximum neither minimum</li> </ul>

### EXAMPLE 1:

Points A[-2, 2] and B[-1, -4] are given. Find the equation of the linear function, draw the graph and find Domain and Range of the function.

Solution:

$$a = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-4 - 2}{-1 - (-2)} = \frac{-6}{-3} = 2 \text{ so I can write } y = ax + b \rightarrow y = 2x + b$$

To find the "b" we can substitute the coordinates of any given point. I'm going to substitute point B [-1, -4]

$$y = 2x + b$$

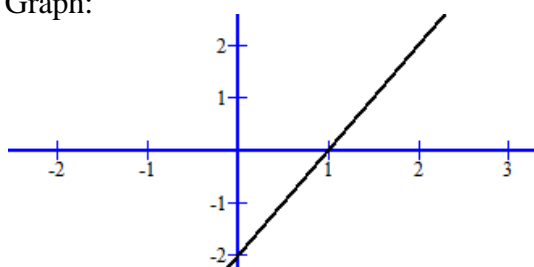
$$-4 = 2 \cdot (-1) + b$$

$$-4 = -2 + b \quad /+2$$

$$-2 = b$$

So now I can write the equation of the function:  $y = ax + b \rightarrow y = 2x - 2$

Graph:



$$D(f) = R$$

$$R(f) = R$$

Increasing

Not bounded

No min, no max

## Exercises 1

State whether each equation or function is linear. Explain.

1.  $y = 3x$

2.  $-\frac{3}{x} + y = 15$

3.  $y = -2 + 5x$

4.  $x = y + 8$

5.  $2x + y = 10$

6.  $g(x) = 8$

7.  $h(x) = \sqrt{x+3}$

8.  $y = 4x^2$

Write each equation in standard form. Identify  $A$ ,  $B$ , and  $C$ .

9.  $y = x$

10.  $y = 5x + 1$

11.  $2x = 4 - 7y$

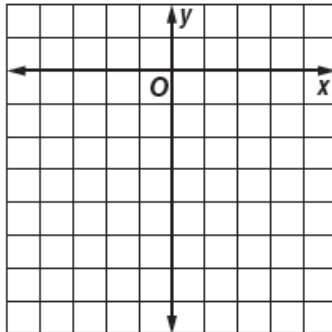
12.  $3x = -2y - 2$

13.  $5y - 9 = 0$

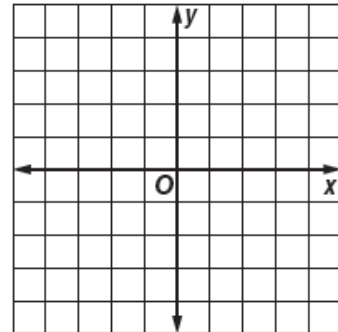
14.  $-6y + 14 = 8x$

Find the  $x$ -intercept and the  $y$ -intercept of the graph of each equation. Then graph the equation using the intercepts.

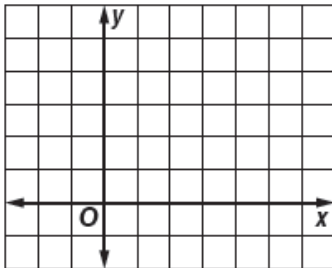
15.  $y = 3x - 6$



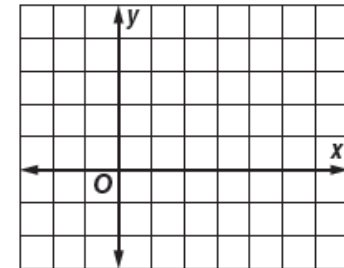
16.  $y = -2x$



17.  $x + y = 5$



18.  $2x + 5y = 10$



## Exercises 2

Find the slope of the line that passes through each pair of points.

1.  $(1, 5), (-1, -3)$

2.  $(0, 2), (3, 0)$

3.  $(1, 9), (0, 6)$

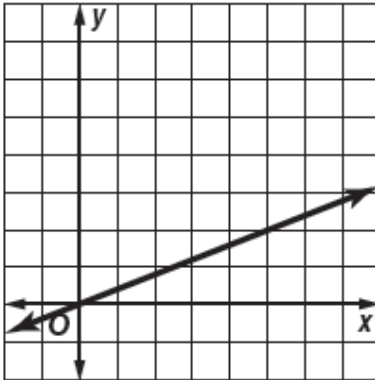
4.  $(8, -5), (4, -2)$

5.  $(-3, 5), (-3, -1)$

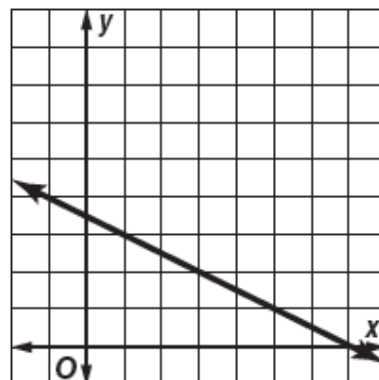
6.  $(-2, -2), (10, -2)$

Find the equation of the linear function from the following graphs.

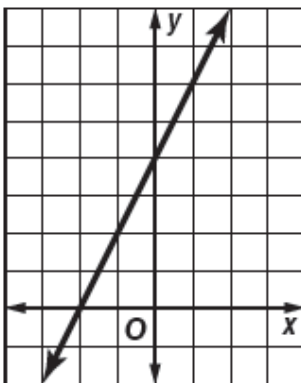
7.



8.



9.



10.

