

Math Worksheet 3 – DOMAIN and RANGE

Given a function $y = f(x)$, the **Domain** of the function is the set of inputs and the **Range** is the set of resulting outputs.

Domains can be found algebraically; ranges are often found algebraically and graphically. Domains and Ranges are sets. Therefore, you must use proper set notation.

Algebraic method:

When finding the domain of a function, ask yourself **what values can't be used**. Your domain is everything else. There are simple basic rules to consider:

- The domain of all polynomial functions is the Real numbers **R**.

$$f(x) = x^3 - 6x^2 + 5x - 11$$

Since $f(x)$ is a polynomial, the domain of $f(x)$ is **R**. It can also be written $(-\infty, \infty)$

- Square root functions can not contain a negative underneath the radical. Set the expression under the radical greater than or equal to zero and solve for the variable. This will be your domain.

$$g(t) = \sqrt{2 - 3t}$$

Since $g(t)$ is a square root, set the expression under the radical to greater than or equal to zero: $2 - 3t \geq 0 \rightarrow 2 \geq 3t \rightarrow 2/3 \geq t$. Therefore, the domain of $g(t) = \left(\frac{2}{3}, \infty\right)$

- Rational functions can not have zeros in the denominator. Determine which values of the input cause the denominator to equal zero, and set your domain to be everything else.

$$h(p) = \frac{p-1}{p^2-4}$$

- Since $h(p)$ is a rational function, the bottom can not equal zero. Set $p^2 - 4 = 0$ and solve: $p^2 - 4 = 0 \rightarrow (p + 2)(p - 2) = 0 \rightarrow p = -2$ or $p = 2$. These two p values need to be avoided, so the domain of $h(p) = \mathbf{R} - \{ -2 \text{ or } 2 \}$ or $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$
The $-$ minus is read as "except".

Graphical method:

Function $y = \sqrt{x + 4}$ has the following graph

The **domain** of the function is $x \geq -4$, since x cannot take values less than -4 .

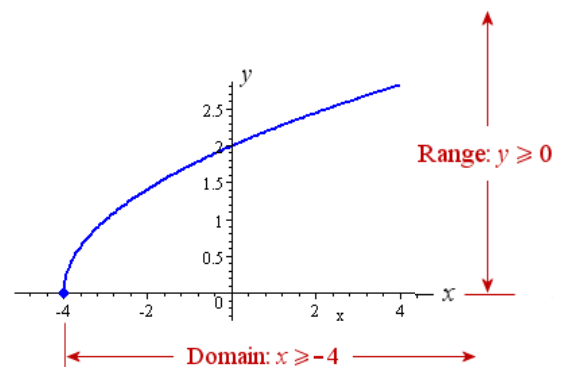
$$D(f) = \langle -4, \infty \rangle$$

The **range** of a function is the possible y values of a function that result when we substitute all the possible x -values into the function.

Make sure you look for **minimum** and **maximum** values of y .

We say that the **range** for this function is $y \geq 0$

$$R(f) = \langle 0, \infty \rangle \text{ (in Slovakia } H(f) = \langle 0, \infty \rangle - \text{obor hodnôt)}$$



Exercises

1. Algebraically determine the following domains. Use correct set notation.

1. $d(y) = y + 3$

2. $g(k) = 2k^2 + 4k - 6$

3. $b(n) = \sqrt{2n - 8}$

4. $m(t) = \sqrt{9 - 3t}$

5. $u(x) = \frac{x - 5}{2x + 4}$

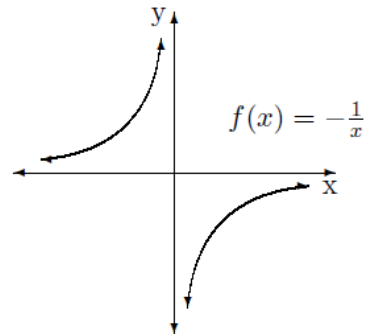
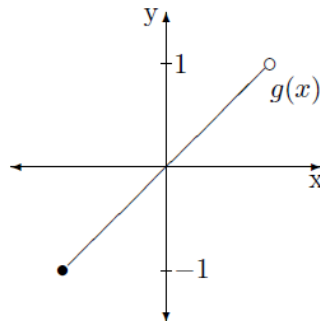
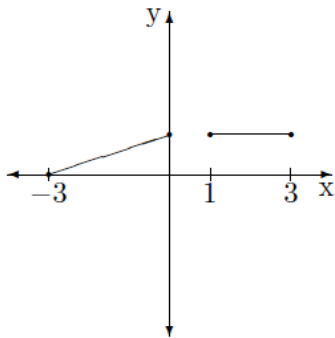
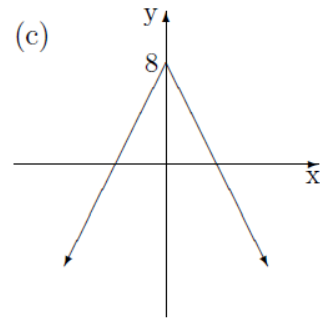
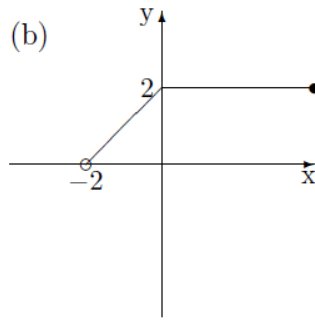
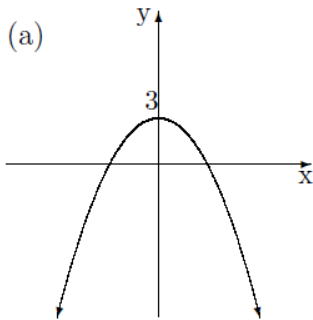
6. $a(r) = r + \frac{1}{r - 1}$

7. $q(w) = \frac{w + 4}{w^2 + 1}$

8.* $f(x) = \frac{x}{\sqrt{x + 3}}$

9.* $t(v) = \sqrt{v^2 + 2v - 8}$

2. Find the domain and range of the following functions from the graph. Use correct set notation



Homework

1. A marathon race was completed by 5 participants. What is the range of times given in hours below?

2.7 hr, 8.3 hr, 3.5 hr, 5.1 hr, 4.9 hr



2. Find the domain

a) $f(x) = \frac{x + 3}{\sqrt{x - 8}}$

b) $g(y) = \sqrt{3y - 54}$

c) $y = \frac{x + 1}{5x + 7}$